

MEASURES AND PROPERTIES OF SHAPES

SECTION 1 Perimeter

SECTION 2 Centimetres and millimetres

SECTION 3 Metres and centimetres

SECTION 4 Area

SECTION 5 3D shapes



MEASURES AND PROPERTIES OF SHAPES

SUGGESTED TIME

5 hours

TEACHING OBJECTIVES

- Suggest suitable units to measure length.
- Measure and draw lines to the nearest millimetre.
- Understand, measure and calculate the perimeter of rectangles and regular polygons.
- Use, read, and write metric units of length, and convert between units.
- Record estimates and measurements from scales to a suitable degree of accuracy.
- Understand area measured in square centimetres.
- Use formula in words for the area of a rectangle. 🗝
- Use all four operations to solve measurement word problems.
- Visualise 3D shapes from 2D drawings and identify nets of an open cube.
 - **SECTION 1** Perimeter
 - **SECTION 2** Centimetres and millimetres
 - **SECTION 3** Metres and centimetres
 - **SECTION 4** Area
 - **SECTION 5** 3D shapes

HOMEWORK

- Several of the Star Challenges are suitable homework activities.
- Learn and use metric units of length, including conversions between units.
- Consolidate multiplication and division by working on area calculations.

Unit 3

Checklist for pupils

Perime	eter	
•	You will: measure lines to the nearest centimetre understand perimeter find perimeters by measuring, counting and calculating solve word problems and puzzles involving perimeter	
Centin	netres and millimetres	
•	You will: measure lines to the nearest millimetre work with measurements given in centimetres and millimetres (cm and mm) or centimetres (cm), to one decimal place add together measurements given in centimetres and millimetres solve word problems using centimetres and millimetres	
Metre	s and centimetres	-
•	You will: work with measurements given in metres (m) and centimetres (cm) add together measurements given in metres and centimetres solve word problems using metres and centimetres	
Area		
•	You will: measure areas by counting squares work out areas measured in square centimetres learn and use the formula for the area of a rectangle	
3D sha	ipes	
	You will: work with drawings of 3D shapes work with nets of an open cube	

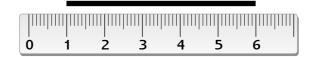
SECTION 1: PERIMETER

DIRECT TEACHING POINTS

• Teach pupils how to measure lengths correctly using a ruler. Model the process pointing out common errors.

Oops and Ouch were asked to measure this line:

Oops put the ruler like this:



This line is 6 cm long.

1 Explain why Oops is wrong:

.....

Ouch put the ruler like this:



What did Ouch do wrong?

Make sure pupils understand perimeter as 'the distance around the edge of a

- Make sure pupils understand perimeter as 'the distance around the edge of a shape'. Exercises 1 and 2 reinforce this idea.
- You need to explain the difference between 'measure' and 'calculate'.
- Star Challenges 1 and 3 provide opportunities for investigative work.



length distance width breadth perimeter centimetre square rectangle equilateral triangle regular pentagon hexagon octagon

Perimeter

Distance round the edge



Measure the distance round the edge of each shape.

Give each answer in centimetres.

Example

5 cm

3 cm

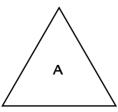
3 cm

16 cm

5 cm

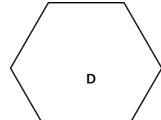
The distance round the edge of this rectangle is:

5 cm + 3 cm + 5 cm + 3 cm = 16 cm



В

C

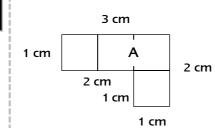


Ε

2 Calculating perimeters



Example



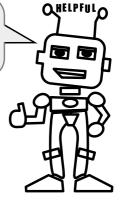
The perimeter of shape A is:

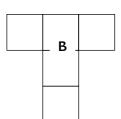
10 cm

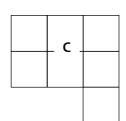
All the shapes below are made from a number of squares joined together. Each square has 1 cm sides.

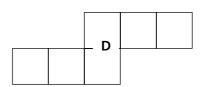
<u>Calculate</u> the perimeter of each of these shapes:

Imagine walking around the outside.

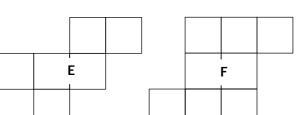


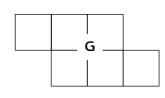






.....





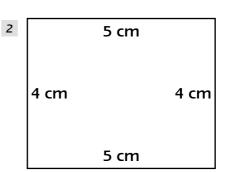
.....

Perimeter

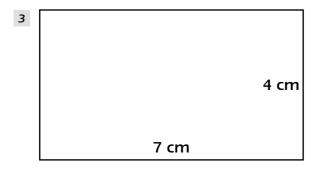
3 Rectangle perimeters



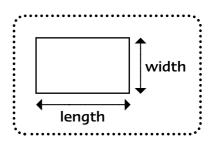
Calculate the perimeter of each of these rectangles:



Perimeter =



Perimeter =



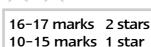
4				
	2 cm			
		8 (cm	

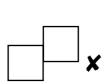
- 5 A rectangle has length 20 cm and width 10 cm. What is its perimeter?
- 6 A square has side 10 cm. What is its perimeter?
- 7 The short side of a rectangle is 3 cm.
 The perimeter is 20 cm.
 What is the length of its long side?

Perimeter

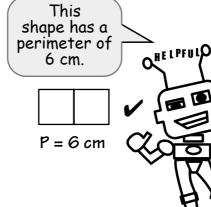


Different perimeters









Use centimetre squared paper.

- Make two different shapes with 3 squares. (2 marks)
 Write down the perimeter of each shape.
- Make five different shapes with 4 squares. (5 marks)Write down the perimeter of each shape.
- Make ten different shapes with 5 squares. (10 marks)
 Write down the perimeter of each shape.

Perimeter



Regular polygons



All correct 1 star

The shapes below are all regular polygons. All the sides are the same length.

Calculate the perimeter of each regular polygon.

Example

square

A square has 4 sides. Each side of this square is 5 cm long.

The perimeter of this square is $4 \times 5 \text{ cm} = 20 \text{ cm}$

20 cm

5 cm

1

regular hexagon

2 cm

A hexagon has sides.

Each side of this hexagon is cm long.

The perimeter of this hexagon is cm.

2

regular pentagon

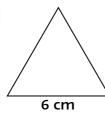
3 cm

A pentagon has sides.

Each side of this pentagon is cm long.

The perimeter of this pentagon is cm.

3



A triangle has sides.

Each side of this triangle is cm long.

The perimeter of this triangle is cm.

4

regular octagon 10 cm

An octagon has sides.

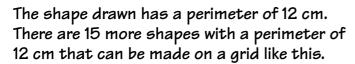
Each side of this octagon is cm long.

The perimeter of this octagon is cm.

Perimeter

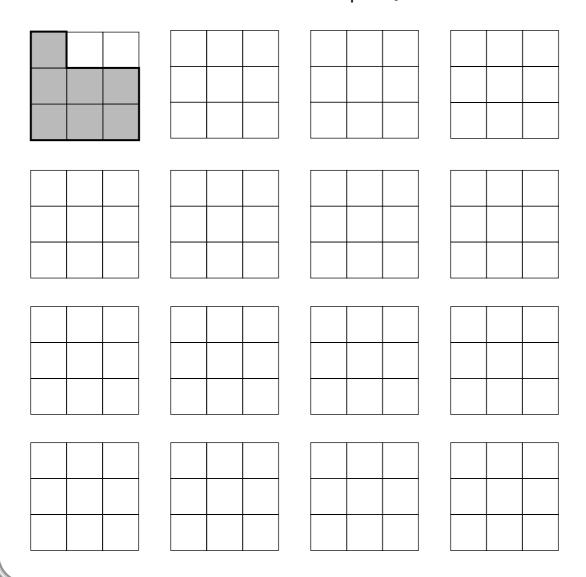


Perimeter puzzle



15 shapes 3 stars 13-14 shapes 2 stars 11-12 shapes 1 star

How many can you find? Rotations and reflections of the same shape only count as 1.





SECTIONS 2 AND 3: CENTIMETRES AND MILLIMETRES METRES AND CENTIMETRES

DIRECT TEACHING POINTS

- Teach the three forms of giving a measurement: mm, cm and mm, and cm using decimals.
- Star Challenge 4 links to work on perimeter.
- Consolidate use of ruler to measure accurately to 1 mm.
- Mental work can concentrate on recall of conversion of units, for example:
 1 km = 1000 m, 1 m = 100 cm, 1 cm = 10 mm, 0.5 m = 50 cm, 24 mm = 2.4 cm,
 112 cm = 1.12 m.
- Teach three forms: cm, m and cm, m using decimals to give measurements.
- Exercise 2 in Section 3 can form the basis of oral mental work. It reinforces complements of 100.
- Use example below as the basis of oral mental problems.

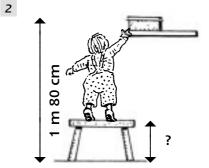
Work out the following:



Paula is standing on tiptoe. She can just reach the light switch.



She stands on a stool. How high can she reach?



She wants to reach the biscuit tin. What is the height of the smallest stool she could use?

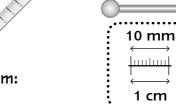


kilometre km metre m centimetre cm millimetre mm

Centimetres and millimetres

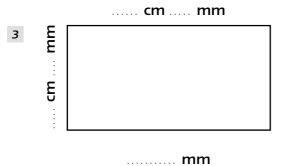
Measuring lines

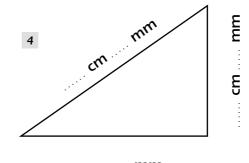
Measure each of these lines to the nearest mm:





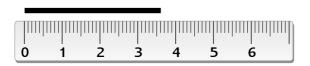
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Longer and shorter lines

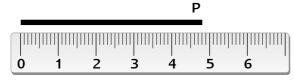
Line A is 3 cm 6 mm long.



(a) Line B is 8 mm longer than A How long is line B?

..... cm mm

Line P is 4 cm 8 mm long.



(a) Line Q is 5 mm longer than P. How long is line Q?

..... cm mm

(b) Line R is 1 cm 1 mm longer than P. How long is line R?

..... cm mm

(c) Line S is 1 cm 1 mm shorter than P. How long is line S?

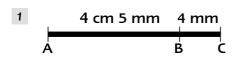
..... cm mm

Centimetres and millimetres

3 Adding cm and mm

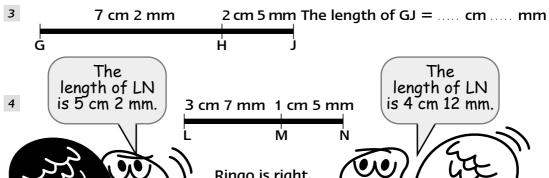
Work out the following.

The diagrams are not drawn to scale.



The length of $AC = \dots cm \dots mm$

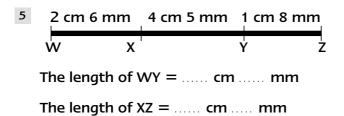
The length of DF = cm mm



Ringo is right.

Bingo is wrong.

Explain why Bingo is wrong.

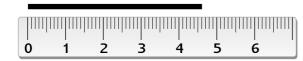


- 6 My pencil is 4 cm 8 mm long. Bob's pencil is 4 mm longer. How long is Bob's pencil?
- 7 I have a zip 10 cm 7 mm long. The zip on my pencil case is twice as long.

 How long is the pencil case zip?

Three ways to measure lines

There are three ways to measure the same line.

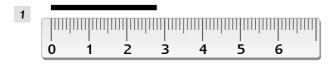


This line is 46 mm long.

This line is 4 cm 6 mm long.

This line is 4.6 cm long.

Measure each of these lines to the nearest mm.



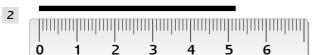
Length of line = mm

10 mm

1 cm

Length of line = cm mm

Length of line = cm



Length of line = cm mm

Length of line = mm

Length of line =cm



Length of line = cm mm

Length of line = cm

Length of line = mm

Length of line = cm

Centimetres and millimetres



Rectangle perimeters

6 correct 2 stars 4-5 correct 1 star

Calculate the perimeter of each shape. Give the answer in cm or in cm and mm.

5 cm

3 cm

Α

P =

6 cm 6 mm

В

3 cm 2 mm

P =

4 cm 8 mm

C

10 cm 2 mm

1 cm 5 mm



P =

2 cm

Ε

cm 5 mm

P =

2 cm 3 mm

2 cm 3 mm

F

P =

P =

Centimetres and millimetres

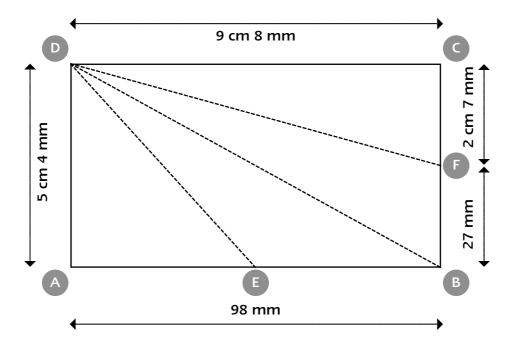


Rectangle measurements

6-7 correct 2 stars

4-5 correct 1 star

ABCD is a rectangle. E is the midpoint of AB. F is the midpoint of BC.



- 1 The length of BC is mm.
- The length of BC can also be written as cm mm.
- AB is 98 mm long. AB is also 9 cm 8 mm long or 9.8 cm long. Write the length of BF in the same three ways.
- 4 Measure DE. Give its length in the same three ways.
- 5 Give the length of DF in the same three ways.
- 6 CE is not drawn, but it can be measured. Is CE the same length as DE?
- AC and EF are not drawn. Is AC twice the length of EF?

Metres and centimetres

	1 Equivale	ent measurements	5		0
Example		4 m 70 cm	 I		1 m = 100 cm
	2 m 40 cm		240 cm	1	
		4.7 m			
Complete	the following	:			
1	2	m 50 cm			
	1 20 cm		cm		
		cm			
		m cn	า		
2					
m	cm			2.8 m	
		560 cm			
3		cm	_		
m	cm		10)5 cm	
		3.25 m			
		750 c	m		_
4					

..... m

..... cm

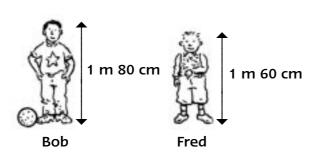
2 m 20 cm

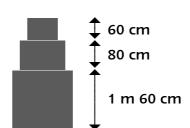
Metres and centimetres

2

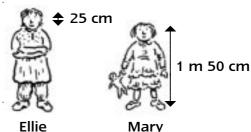
Measurement problems

- 1 m = 100 cm
- 1 What length do I add to 70 cm to make 1 m?
- What length do I add to 25 cm to make 1 m?
- 3 What length do I add to 2 m 50 cm to make 3 m?
- 4 What length is 10 cm less than 1 m?
- 5 What length is 25 cm less than 1 m?
- 6 How high is the tower?





- Bob is taller than Fred. How much taller is he?
- 8 Ellie is 25 cm taller than Mary. Mary is 1 m 50 cm. How tall is Ellie?



- 9 Carl's desk is 90 cm long.His bookshelf is twice as long as his desk.How long is his bookshelf?
- I need two pieces of wood for my project. The long piece is 2 m 30 cm long. The short piece is half the length of the long piece.

How long is the short piece?

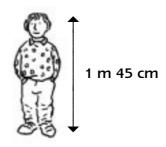
Metres and centimetres

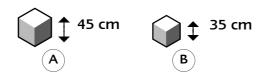


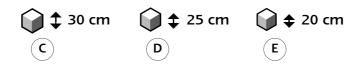
Petros' tower

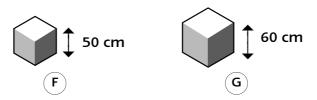


4 correct 2 stars 3 correct 1 star









Petros wishes to build a tower of cubes exactly as tall as himself.

- 1 Which three different cubes could he use?
- Which four different cubes could he use?
- Find another combination of four cubes he could use.
- What is the height of the tallest tower of cubes he could build using five different cubes only?

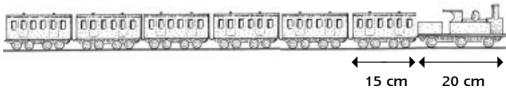
Metres and centimetres



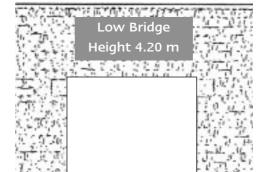
Trains and lorries



- 1 (a) What is the total length of the toy lorry and trailer in cm?
- 45 cm 60 cm
- (b) What is its total length in m and cm?
- (c) What is its total length in m?
- 2 A toy train has an engine and six identical carriages.



- (a) What is the total length of the train in cm?
- (b) What is its total length in m and cm?
- (c) What is its total length in m?



- A lorry is 3 m 70 cm tall. It goes under this low bridge.
 - What is the size of the gap between the top of the lorry and the bridge?



SECTION 4: AREA

DIRECT TEACHING POINTS

- Clarify the meaning of 'area'. Exercises 1 and 2 are consolidation exercises.
- Consolidate multiplication and division using area calculations, for example, $6 \times \square = 30$.
- Applications include finding the area of compound figures and right-angled triangles, for example, exercise 5 and Star Challenge 10.
- Star Challenge 9 can be extended to include other perimeters.



area square centimetre cm² square metre m²

Area

1 What is area?

The area of a shape is how much space it covers.

The area of this shape is 4 squares.

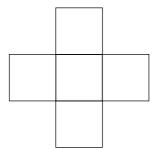
Write down the area of each shape.

1

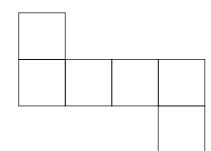
Area = 4 squares

Area = squares

2



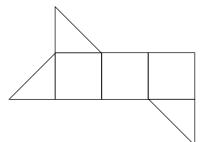
3



Area = squares

Area = squares

4



Area = squares

Area

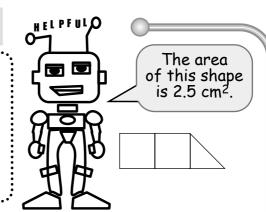
2 Square centimetres

1 cm

1 cm

The most common unit of area is the square centimetre.

Area =1 cm²



Write down the area of each shape. Each answer must have the correct units.

1



Area = cm²

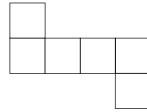
2



Area = cm^2

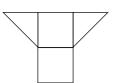
3

6



Area = cm^2

4



Area = cm^2

5

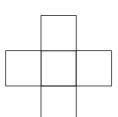


Area =

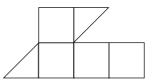


Area =

7



8

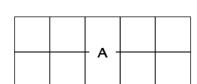


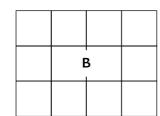
Area =

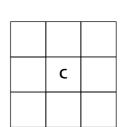
Area =

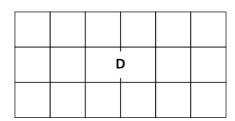
Area

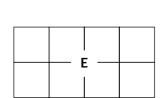
3 Areas of rectangles

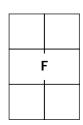






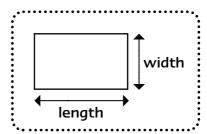






- G rectangle with length = 10 cm width = 4 cm
- H rectangle with length = 6 cm width = 5 cm
- 1 Complete this table for rectangles A, B, C, D, E, F, G, H.

Rectangle	Length in cm	Width in cm	Area in cm²
Α	5	2	
В			
С			
D			
E			
F			
G	10	4	
Н	6	5	



Area

The rule for the area of a rectangle

Area of rectangle = length × width

Use the rule to work out the area of each rectangle. Each answer must have the correct units.

1

	5 cm
10 cm	

Area = \dots cm²

2

8 cm

3

	2 cm
15 cm	

Area =

Area	=	

8 cm

Area problems

Work out these problems. Use the correct units in each answer.

- 1 What is the area of a rectangle of length 20 cm and width 3 cm?
- 2 A rectangle has width 5 cm. The length is twice the width. What is the area of the rectangle?
- What is the area of a square with 5 cm sides?

Area = 20 cm^2 10 cm

What is the width of this rectangle?

5 What is the length of the

Area = 36 cm² side of this square?

⁶ The area of triangle A is half the area of rectangle B. What is the area of triangle A?



12 cm

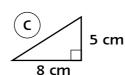
10 cm

В	

12 cm

10 cm

7 What is the area of triangle C?



3

PART 3 UNIT 3 SECTION 4

Area



Measure and work out the area



6-7 correct 1 star

For each rectangle:

- measure the length and width
- work out the area.
- work out the perimeter

(A)	
	Area =
	P =

Area



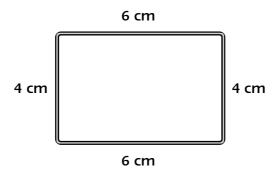
Wire rectangles

XO

Imagine that you have a piece of wire 20 cm long.

It could make this rectangle.

6-8 marks 1 star 1 mark for each correct rectangle and 1 mark for each correct area



Sketch four more different rectangles that you could make with this wire.

Write the length and width on each rectangle.

Inside each rectangle, write its area.



Remember: a sketch is not an accurate drawing.

3 National Strategy

Area



Units of area

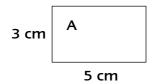


9-10 correct 1 star

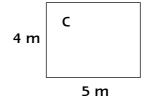
Work out the area of each of these shapes.

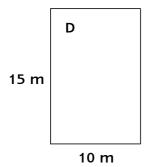
They are not drawn to scale.

Each answer must have the correct units.

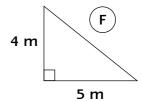


4 cm 6 cm

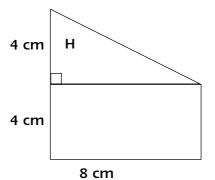


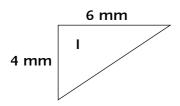


2 mm E 3 mm









Remember: these shapes are not drawn to scale.





SECTION 5: 3D SHAPES

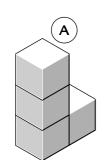
DIRECT TEACHING POINTS

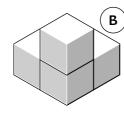
- Some pupils will need a practical approach to solving the problems.
- Star Challenges 11 and 12 can form the basis of a class discussion use an OHT of the shapes to help guide the discussion.

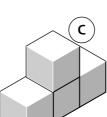


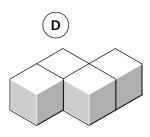
3D shapes

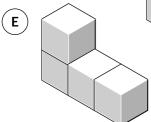
1 Drawings of 3D shapes

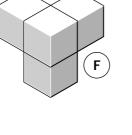


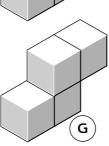


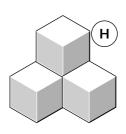












Each of these shapes has been made with four cubes.

same shapes.

1 Work out which drawings

are different views of the

..... = =

A =

..... =

2 Make each shape. Use your shapes to check whether your answers are right.

2

Nets of open boxes

Here are some nets.

1 For each net,
decide whether
it will fold up to
make an open box.
Under each net,
write 'Yes'
or 'No'.





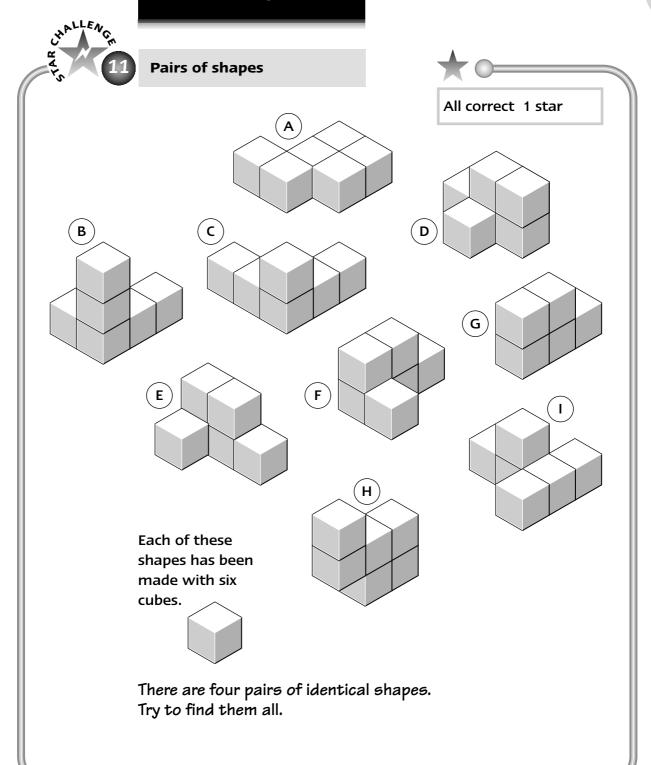






For each 'Yes', shade the square that is at the bottom of the open box.

3D shapes



3D shapes

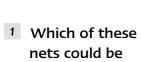


Mind the paint

*0

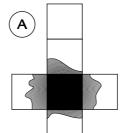
All correct 1 star

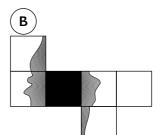
This cube has been standing in a pool of paint.

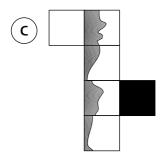


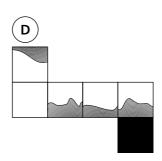
this cube?

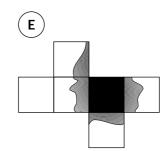
.....





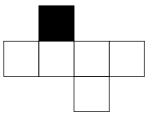






2 For this net, the painted face is shown.

Copy the net and shade in the edges of the four faces that are also painted.



Section 1 Perimeter

- Distance round the edge
 - (A) 9 cm (B) 14 cm (C) 12 cm (D) 12 cm (E) 12 cm
- Calculating perimeters
 - (A) 10 cm (B) 12 cm (C) 12 cm (D) 14 cm (E) 14 cm
 - (F) 14 cm (G) 12 cm
- Rectangle perimeters
 - 1 18 cm 2 18 cm 3 22 cm 4 20 cm 5 60 cm
 - 6 40 cm 7 7 cm

Section 2 Centimetres and millimetres

- Measuring lines
 - 1 46 mm; 4 cm 6 mm
 - 2 5 cm 9 mm; 59 mm
 - 2 cm 8 mm 28 mm

54 mm

6 cm 1 mm 3 cm 5 mm

- Longer and shorter lines
 - 1 (a) 4 cm 4 mm
 - 2 (a) 5 cm 3 mm (b) 5 cm 9 mm
- (c) 3 cm 7 mm

Centimetres and millimetres

continued

3

Adding cm and mm

- 1 4 cm 9 mm
- 2 5 cm 9 mm
- 3 9 cm 7 mm
- 4 12 mm should be changed to 1 cm 2 mm
- 5 WY = 7 cm 1 mm XZ = 6 cm 3 mm
- 6 5 cm 2 mm
- 7 21 cm 4 mm

4

Three ways to measure lines

- 1 28 mm;
- 2 cm 8 mm;
- **2.8** cm

- ² 5 cm 2 mm;
 - 52 mm;
- **5.2** cm

- 3 71 mm
- 4 5 cm 3 mm
- 5 **6.5** cm

- 6 74 mm
- 7 **2.7** cm

Section 3

Metres and centimetres

1

Equivalent measurements

1 20 cm

2

2 m **80** cm

5 m **60** cm

- 3
- **325** cm
- 4

1 m 5 cm

220 cm

7.5 m

2

Measurement problems

- 1 30 cm
- ² 75 cm
- ³ 50 cm

- 4 90 cm
- ⁵ 75 cm
- 6 3 m

- ⁷ 20 cm
- ⁸ 1 m 75 cm
- ⁹ 1 m 80 cm

¹⁰ 1 m 15 cm

Section 4

Area

- What is area?
 - 1 3 squares 2 5 squares 3 6 squares 4 4½ squares

- Square centimetres
 - 1 2 cm²
- 2 4 cm²
- 3 6 cm²
- 4 3 cm²

- **5 3.5** cm²
- 6 4 cm²
- **7 5** cm²
- **8 5** cm²

Areas of rectangles

1	Rectangle	Length in cm	Width in cm	Area in cm²
	Α	5	2	10
	В	4	3	12
	C	3	3	9
	D	6	3	18
	E	4	2	8
	F	2	3	6
	G	10	4	40
	Н	6	5	30

- The rule for the area of a rectangle
 - 1 50 cm²
- **2 64** cm²
- **3** 30 cm²

- Area problems
 - 1 60 cm²
- ² 50 cm²
- ³ 25 cm²
- 4 2 cm

- ⁵ 6 cm
- 6 60 cm²
- 7 20 cm²

Section 5

3D shapes

- **Drawings of 3D shapes**
 - A = E
- D = G
- B = F = H
- Nets of open boxes
 - 1 (A) Yes
- (B) Yes
- (c) Yes
- (D) No













PART 3 UNIT 3 ANSWERS

Unit 3 Answers



Star Challenge answers

Different perimeters

16-17 marks 2 stars 10-15 marks 1 star

1



$$P = 8 \text{ cm}$$
 $P = 8 \text{ cm}$

2











3 Any **ten** of these shapes:









$$P = 12 \text{ cm}$$
 $P = 10 \text{ cm}$ $P = 12 \text{ cm}$

$$P = 12 cm$$









$$P = 12 \text{ cm}$$
 $P = 12 \text{ cm}$









P = 12 cm

P = 12 cm

P = 12 cm P = 12 cm







Regular polygons

All correct 1 star

- 1 A hexagon has 6 sides. Each side of this hexagon is 2 cm long. The perimeter of this hexagon is 6 × 2 cm = 12 cm
- 2 A pentagon has **5** sides. Each side of this pentagon is **3** cm long. The perimeter of this pentagon is **5** × **3** cm = **15** cm
- A triangle has 3 sides.

 Each side of this triangle is 6 cm long.

 The perimeter of this triangle is 3 × 6 cm = 18 cm
- 4 An octagon has **8** sides. Each side of this octagon is **10** cm long. The perimeter of this octagon is **8** × **10** cm = **80** cm

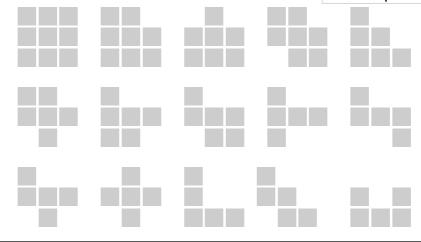


Star Challenge answers

continued



15 shapes 3 stars 13-14 shapes 2 stars 11-12 shapes 1 star





Rectangle perimeters

6 correct 2 stars 4-5 correct 1 star

- 16 cm
- 19 cm 6 mm
- 30 cm



Rectangle measurements

6-7 correct 2 stars 4-5 correct 1 star

- 1 54 mm
- 2 5 cm 4 mm

9.2 cm or 9 cm 2 mm

- ³ 27 mm;
- 4 73 mm;
- 2 cm 7 mm;
- 2.7 cm

- 7 cm 3 mm;
- 7.3 cm

- ⁵ 102 mm;
- 10 cm 2 mm;
- 10.2 cm

⁷ Yes; AC = 112 mm and EF = 56 mm



Petros' tower

4 correct 2 stars

- ¹ B, F, G
- ² and ³ A, C, E, F and B, C, E, G

4 2 m 20 cm or 220 cm

6 Yes; both are 73 mm



Trains and lorries

All correct 1 star

- ¹ (a) 105 cm
- (b) 1 m 5 cm
- (c) 1.05 m

- (a) 110 cm
- (b) 1 m 10 cm
- (c) 1.1 m

³ 50 cm

PART 3 UNIT 3 ANSWERS

Unit 3 Answers



Star Challenge answers

continued

Measure and work out the area

6-7 correct 1 star

- (A) 8 cm²
- (B) 6 cm²
- (c) 12 cm²
- 16 cm²

- P = 12 cm
- P = 10 cm
- P = 14 cm
- P = 20 cm

- (E) 21 cm²
- (F) 40 cm²
- 9 cm²

- P = 20 cm
- P = 26 cm
- P = 12 cm



Wire rectangles

6-8 marks 1 star

The expected rectangles and their areas:

Length 2 Width 5 9 16 Area



Units of area

9-10 correct 1 star

- (A) 15 cm²
- (B) 24 cm²
- (c) 20 m²
- (D) 150 m² (E) 6 mm²

- (F) 10 m²
- 22 m²
- (H) 48 cm²
- (I) 12 mm²



Pairs of shapes

All correct 1 star



B and **C A** and **H**

D and **G**

E and F

Mind the paint

All correct 1 star

1 A, B, E



